



# A Study on Cooling Rate Modelling of Dendrite between the Temperature and Composition in TiAl Intermetallic Compounds

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## Abstract

According to composition at solid and liquid interface in solidification the line model of temperature and composition in dendrite has been established. The equation is gained as  $T = -1000C + 2273$ . Meantime the cooling rate and time has been discussed. In the intersection the cooling rate of solid and liquid  $\Delta T$  is gained. According to dendrite therefore the composition can determine temperature. Y changes from pure X to pure Y ie. 0 to 100%Y the temperature will change from maximum to minimum at Al composition in materials like TiAl. The period one of cooling rate is from 0.5K/s to 29 K/s in speed of 2060mm/hr. The gap is bigger between 1560mm/h with drawing speed  $v$  than that of 1060mm/h. For engineering use the speed is better when the speed is higher like 2060mm/h when the cooling rate attains from 0.4K/s to 29K/s with the composition difference increasing with the maximum value. When cooling rate is 2060mm/hr the biggest one in these three conditions will happen with 29K/s when it is pure Al. When DS is 2J/(mol•K) the DG changes from 1500J to -500J with the temperature increases same in TiAl. It means that when DS becomes big the DG will decrease. From diagram the concentration of Al is measured to be 1.6at% in 46Al at%. The calculation value is thought to be phase forming element due to the minus. That has been the low concentration with and solid solution in TiAl.

**Keywords:** Modelling; TiAl; Dendrite; Analysis; Temperature; Cooling rate; Composition; Interface; Gibbs free energy

## Introduction

The change of temperature in the solid and liquid in solidification transformation can deduce the their related formula. The curve expresses its trend better. From this relation their composition will change when the transformation happens. It is known that the temperature in solidification can solve their relationship. In this study in terms of these equations the deduction and analysis is done and the error analysis to them is done. Here the solid and liquid equation is explored within line and find the simple formula which make us to calculate the cooling rate rapidly [1,2]. Therefore in this study the model of temperature and composition has been established to observe the trend and intrinsic relationship between them. Then the error is checked with variance to both of

constant. TiAl as a promise materials has been searched and developed for many years. However the cooling rate with compositions is not much yet, so in this study the equation is established through temperature and composition according to the phase diagram. It is modelled with cooling rate and composition difference too in directional solidification test. The detail value is combined through phase equilibrium line and it is compared with thermal dynamics. The research scope is from 0 to pure Al here [2]. On the other side the relationship with cooling rate and energy difference & temperature has been investigated according to varied speed and  $\Delta S$  respectively for the application. According to the solidified crystalline and phase diagram the application will be known. In addition relationship between cooling rate and energy difference & temperature are drawn for

further research in this study. To calculate the cooling rate is our destination in the end in terms of the composition in TiAl alloys. Therefore the establishment equation between temperature and cooling rate in terms of the equilibrium diagram [3-5].

### Calculation

#### The relationship between composition and temperature (Figure 1)

Figure 1 shows that the two lines with liquid and solid phase meet in one point. The cooling rate  $\Delta T$  is known.

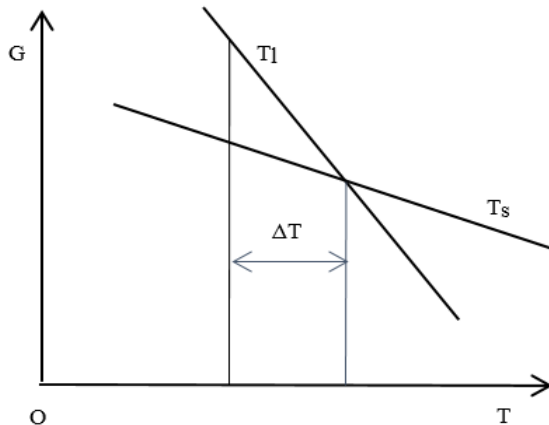


Figure 1: The relations of dendrite and equilibrium state.

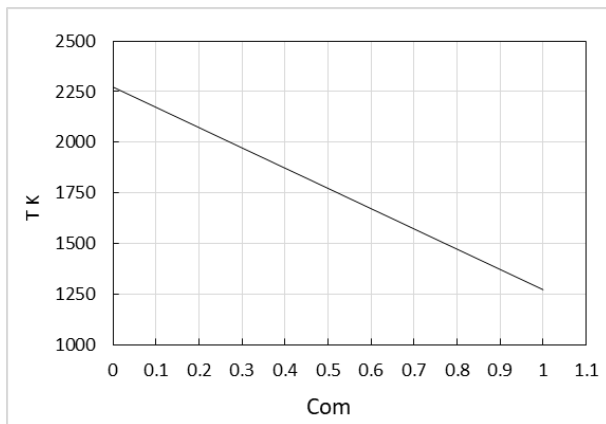


Figure 2: The relationship between temperature ad compositions in dendrite.

It shows two phases decrease below the liquids phase line. It shows these two line relations in constitutional super cool. We choose the certain value to proceed experiment. Here C is the Al composition,  $C_l$  and  $C_s$  is the liquid and solid composition of Al.

$$\text{Let } T = aC + b \quad (1)$$

We have

$$T_l = aC_l + b \quad (2)$$

$$T_s = aC_s + b \quad (3)$$

According to Ti-Al state equilibrium state we have supposed

$$C_l = 0.44, T_l = 1833K \text{ and}$$

$$C_s = 0.46, T_s = 1813K$$

Substitute above constant to (2) and (3), so

$a = -1000, b = 2273$ . The formula (1) is

$$T = -1000C + 2273 \quad (4)$$

This is the equation to calculate temperature in terms of composition (Figure 2).

From Figure 2 we know the distribution of temperature and composition in directional solidification. When composition difference increases temperature decreased somewhat in term of content in dendrite. When composition difference is from 0 to 1 the temperature changes from 2300K to 1300K respectively. It means Y changes from pure X to pure Y ie. 0 to 100%Y the temperature will change from maximum to minimum at Al composition in materials like TiAl.

#### Calculation of cooling rate (Figure 3)

As Figure 3 when composition difference increases cooling rates rate increases properly at 20mm solidified length with the drawing speed from 1060mm/hr, 1560mm/hr and 2060mm/hr. Drawing speed increases so that cooling rate increases a certain. The period one of cooling rate is from 0.5K/s to 22 K/s in speed of 1560mm/hr. The gap is bigger between 1560mm/h with drawing speed  $v$  than that of 1060mm/h. For engineering use the speed is better when the speed is higher like 2060mm/h. When the cooling rate attains from 0.5K/s to 29K/s with the composition difference increasing with maximum value in speed of high value. When cooling rate is 2060mm/hr the biggest one in these three conditions will happen with 29K/s. This is the result of concentration of liquid and solid in terms of composition.

$$\Delta T = T_l - T_s = -1000(C_l - C_s) = -150K \quad (5)$$

$$t = L/v = 20 * 3600 / 360 = 200s$$

$$\text{So } C = (T_l - T_s) / t \quad (6)$$

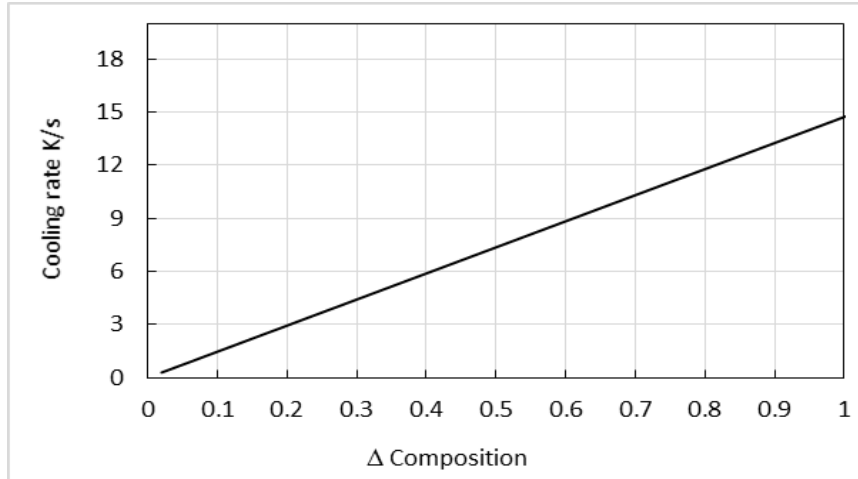
Here C and  $\Delta T$  is cooling rate and temperature difference respectively (Figure 4).

From Figure 4 DG decreases with temperature increasing. It decreases with entropy DS increasing from 1, 2 to 2J/mol/K. It's decreasing means cooling rate increases along the dendrite. When speed increases it decreases like 1560mm/h. This is the result of concentration of liquid and solid in terms of composition. When DS is 1.2J/ (mol•K) the DG changes from 2200J to 1000J with the temperature increases from 850K to 1900K respectively. When DS is 2J/ (mol•K) the DG changes from 1500J to -500J with the temperature increases same. It means that in TiAl when DS becomes big the DG will decrease. G is Gibbs free energy and DH is enthalpy [3]. It is supposed that enthalpy is constant in this study.

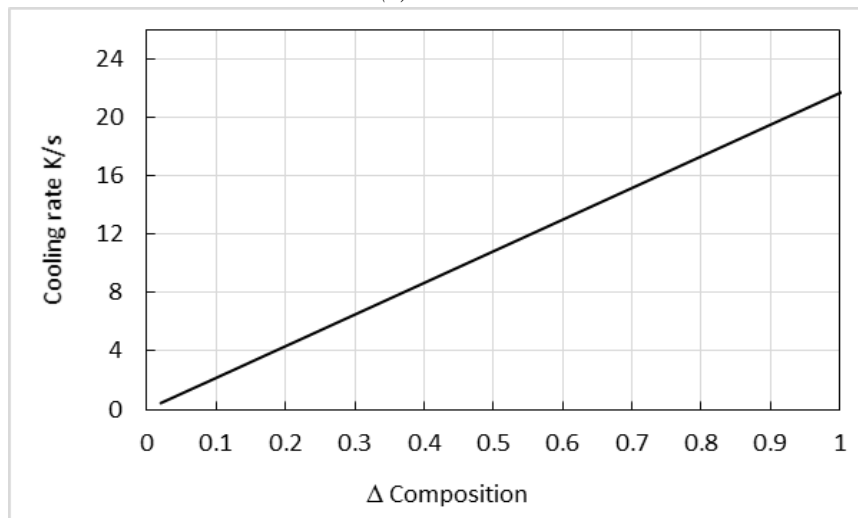
$$DG = DH - TDS \quad (7)$$

In Ti-Al DH and DS are to be

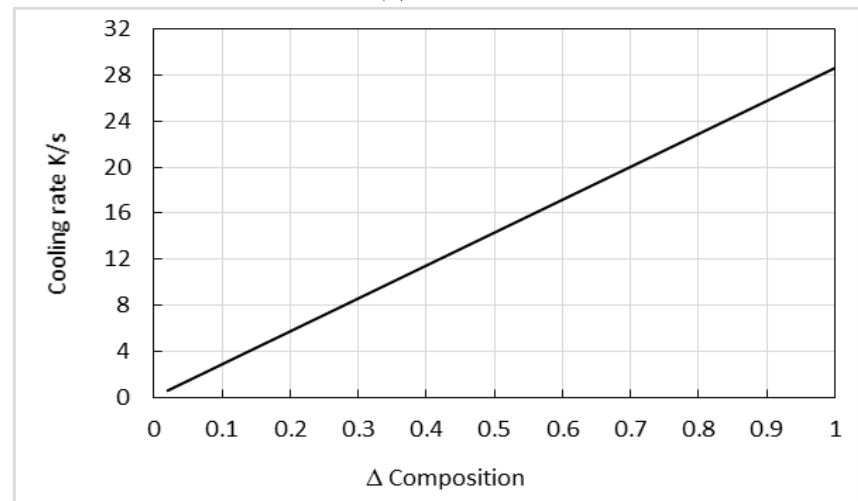
$$DH = 3.3KJ/mol, DS = 1.2 J/mol/K \text{ at } 1492^\circ C \quad [4] \text{ (Figure 5).}$$



(a) 1060mm/hr.

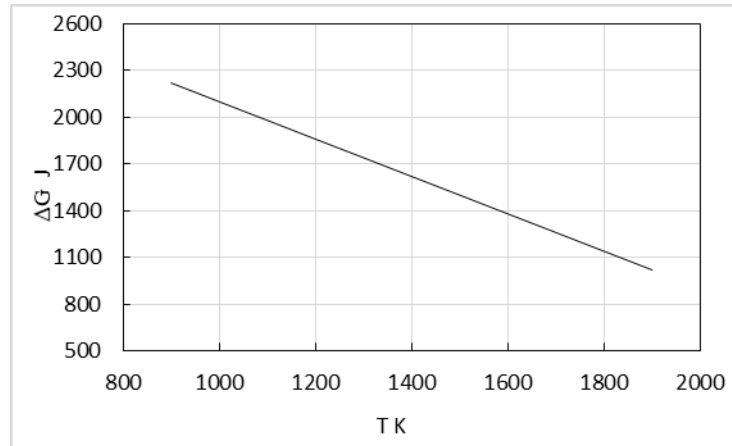


(b) 1560mm/hr.

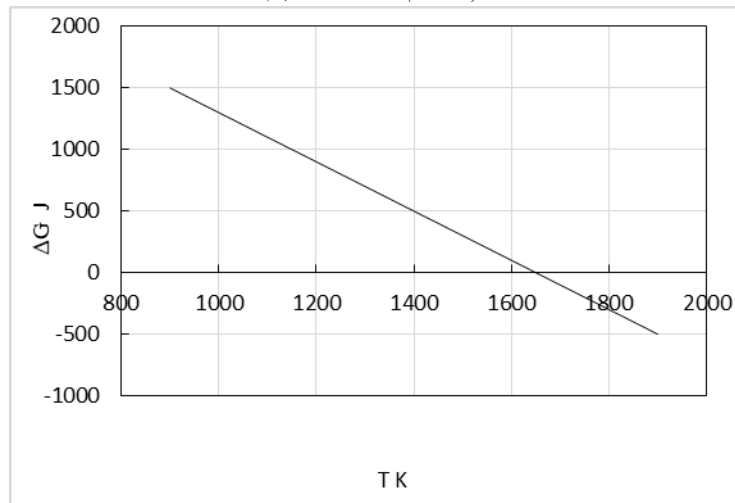


(c) 2060mm/hr.

**Figure 3:** The relation between cooling rate and  $\Delta$  composition under different speed in directional solidification.

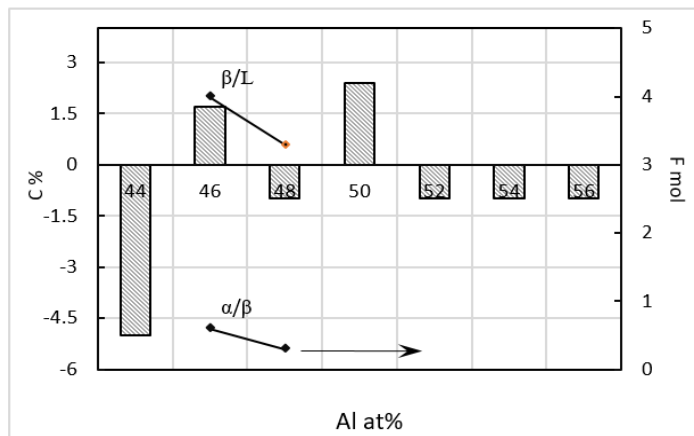


(a)  $DS=1.2J/(mol\cdot K)$ .



(b)  $DS=2J/(mol\cdot K)$ .

**Figure 4:** The relations between  $DG$  and temperature in solidified state.



**Figure 5:** Trend  $F_{mol}$  and  $C_{Al}$  with Al content in  $\gamma$  TiAl,  $\beta$  and  $\alpha$  is formed and L is remained [5].

The concentration of Al under the reaction will be known in Figure 5. The interface stability is highly expected because of the constitutional supercooling. Well-developed dendrites are found at relatively high solidification rate with 25~100 $\mu$ m/s. As for 44Al



at% it uses  $\beta \rightarrow \alpha \rightarrow \alpha + \gamma$  to measure Al concentration while for above 46Al at% it uses  $\beta \rightarrow \gamma$ . From the line it will be increased from 44 to 56 Al at% for  $\beta$  phase. From diagram the concentration of Al is measured to be 1.6at% in 46Al at%. The calculation value is thought to be phase forming element due to the minus. That has been the low concentration with and solid solution in TiAl. Maybe good result will be obtained use the inferior solution model. They agreed with each other well [4]. So they are approximate value calculated with the method.

## Conclusions

- According to composition at solid and liquid interface in solidification the line model of temperature and composition in dendrite has been established. The equation is gained as  $T = -1000C + 2273$ . Meantime the cooling rate and time has been discussed. In the intersection the cooling rate of solid and liquid  $\Delta T$  is gained. Composition difference has been deduced and analysed according to dendrite therefore the composition can determine temperature. When composition difference is from 0.4 to 0.6 the temperature changes from 1880K to 1680K. Y changes from pure X to pure Y ie. 0 to 100%Y the temperature will change from maximum to minimum at Al composition in materials like TiAl.
- The period one of cooling rate is from 0.5K/s to 29 K/s in speed of 2060mm/hr. The gap is bigger between 1560mm/h with drawing speed  $v$  than that of 1060mm/h. For engineering use the speed is better when the speed is higher like 1160mm/h when the cooling rate attains from 0.3K/s to 29K/s with the composition difference increasing with maximum value. When cooling rate is 2060mm/hr the biggest one in these three conditions will happen with 29K/s.
- When DS is 2J/ (mol•K) the DG changes from 1500J to -500J with the temperature increases same. It means that in TiAl alloys when DS becomes big the DG will decrease. From diagram the concentration of Al is measured to be 1.6at% in 46Al at%. The calculation value is thought to be phase forming element due to the minus. That has been the low concentration with and solid solution in TiAl.

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